



# Calibration of the GISSMO model using LS-OPT®

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# Overview

- Goals
- Background
- Theory of DTW
- Example
- Conclusions
- Recommendations

# Goal

- To demonstrate the ability to calibrate a GISSMO model using 3 test cases
  - Characteristics
    - Computational noise
    - Steep failure curves
- To establish a best practice for GISSMO model characterization using LS-OPT®

# Background

- As a result of requests for assistance with GISSMO calibration as well as a demand for supporting DIC as part of the calibration procedure we have recently also added new, more robust, curve similarity measures namely Dynamic Time Warping (1994) and Discrete Fréchet (1906).

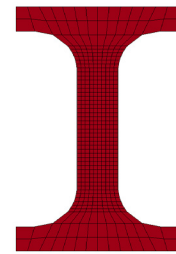
# Setup and Example Overview

- Parameters: 7
- Test cases: 3
- Target curve: Synthetic
- Curve Matching

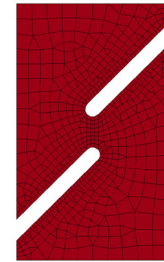
- Dynamic Time Warping (DTW) (1994)
- Truncation of Force history at failure load (uses LS-OPT feature)

- Optimization methods

- SRSM (Sequential Response Surface, local optimizer): 15 iter, 14 sim, 3 cases = 639
- GA (Direct Genetic Algorithm, global optimizer): 50 gen, 100 pop., 3 cases = 15000



Tensile



Shear



Tensile (notch)

# Dynamic Time Warping

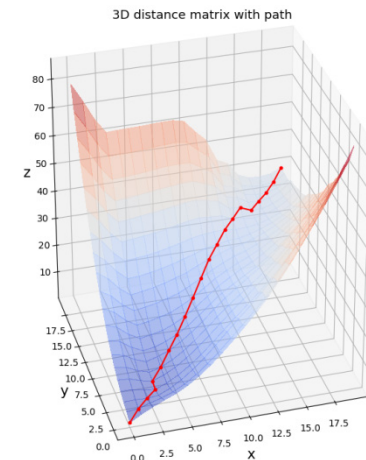
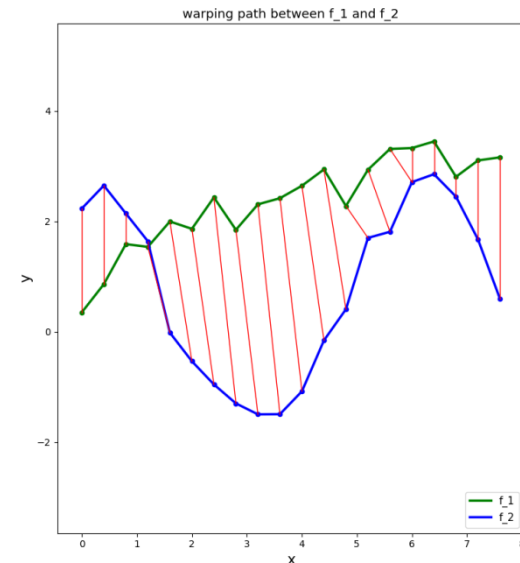
## Curve Similarity Measure

DTW calculates the distance between two data sets, which may vary in time, via its corresponding **warping path**. This path is the result of the **minimum accumulated distance** which is necessary to traverse all points in the curves

While the Euclidean distance measure is a strict **one-to-one** mapping, DTW also allows **one-to-many** mappings.

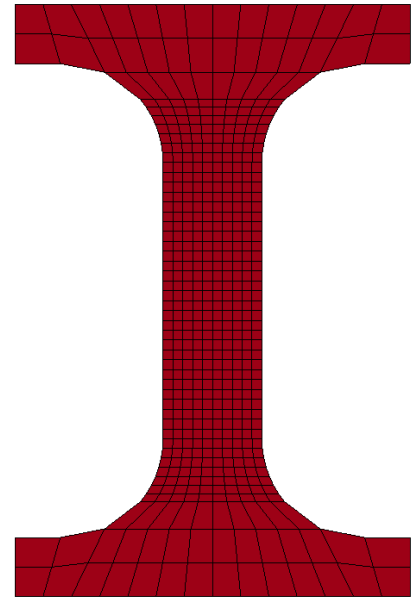
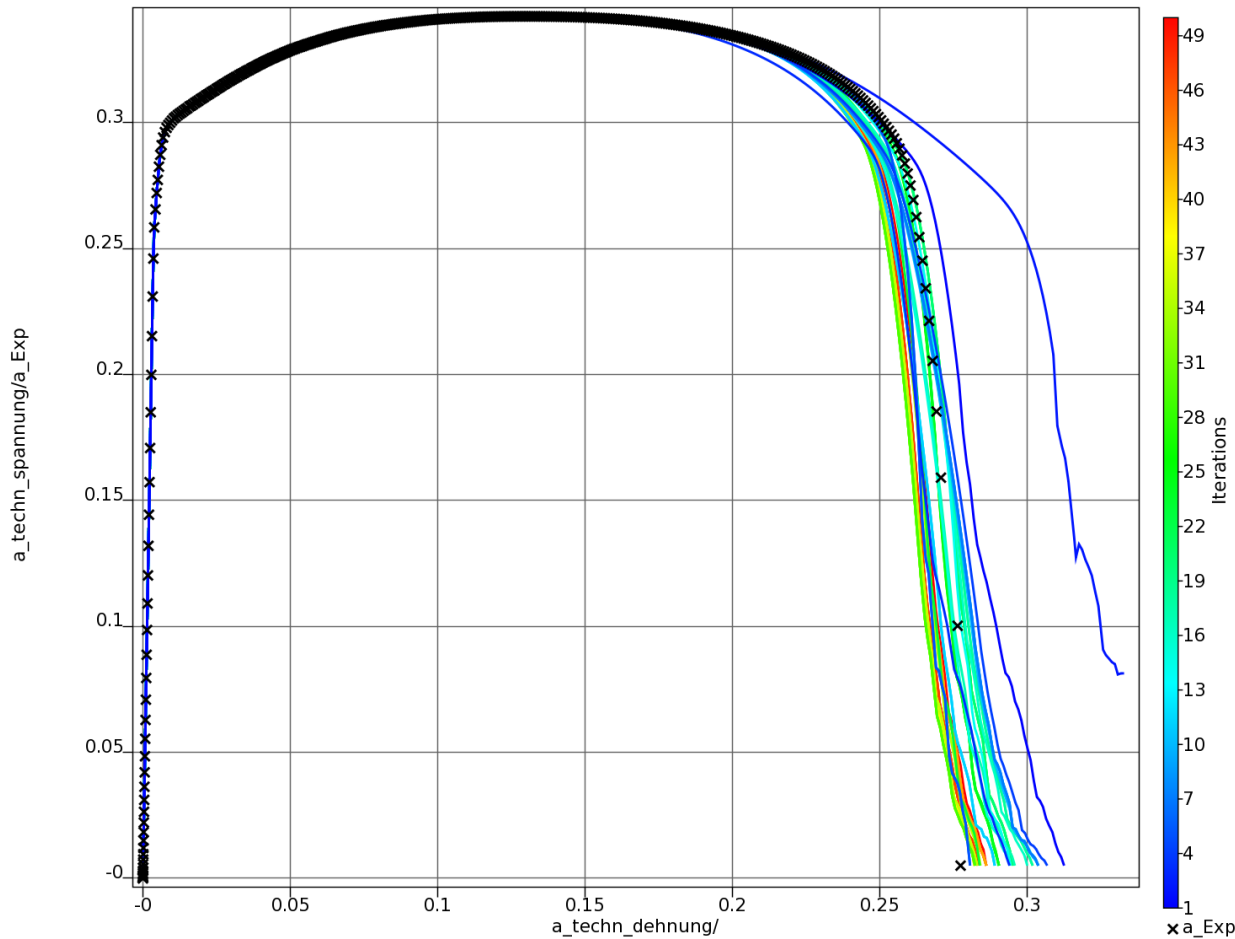
Mathematically,

$$DTW(P, Q) = \min_W \left\{ \sum_{i=1}^l \delta(w_i) \right\}$$



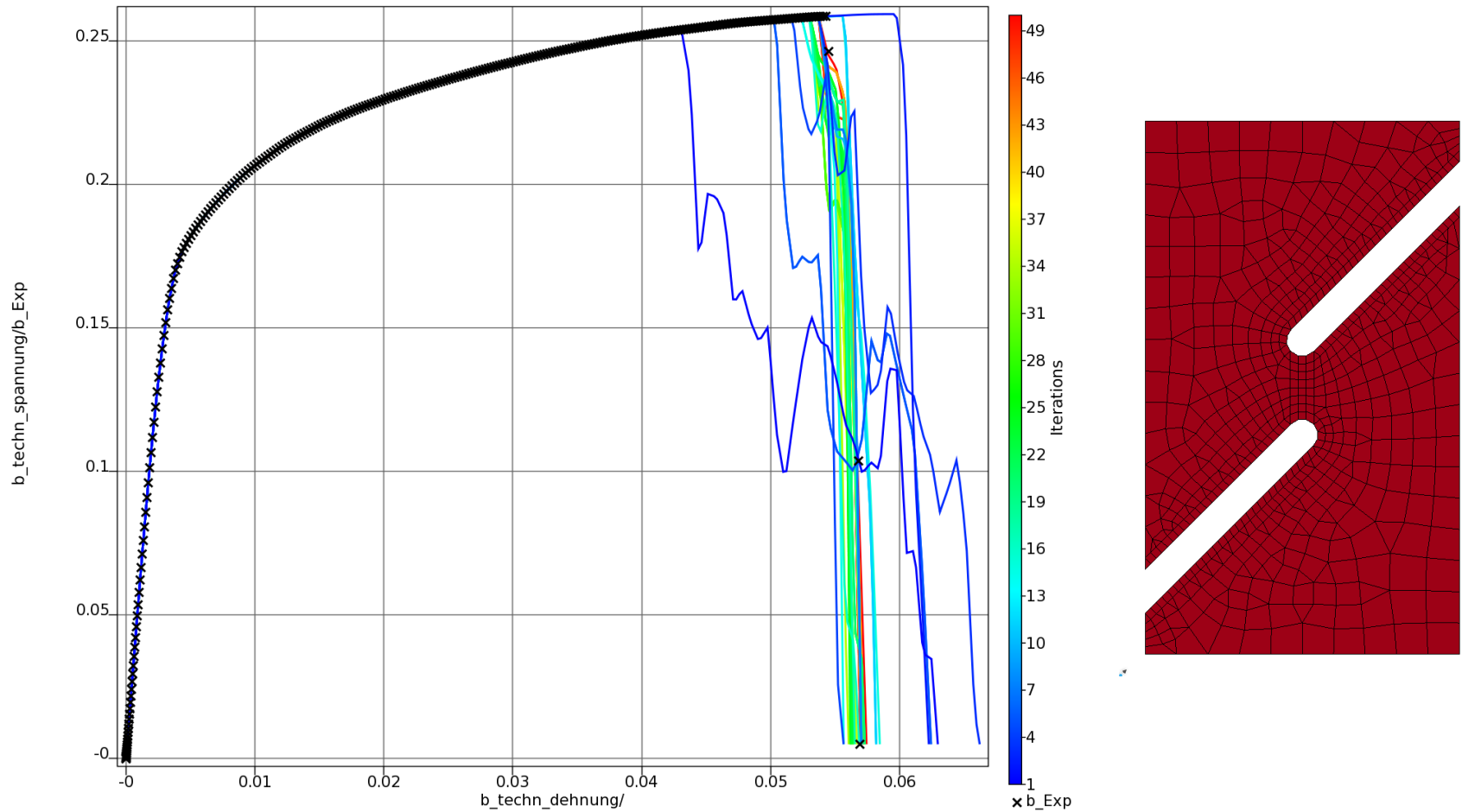
# Case A: tensile

## GA: optimum at each generation



# Case B: shear

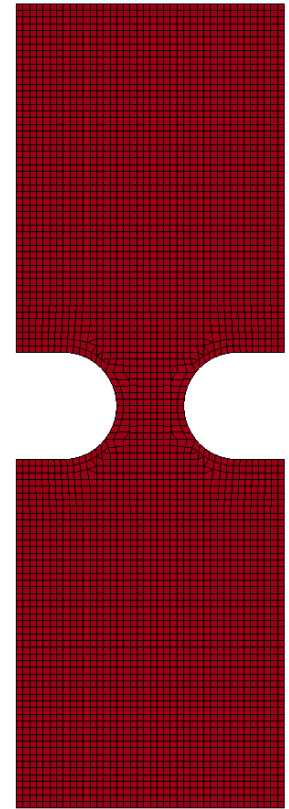
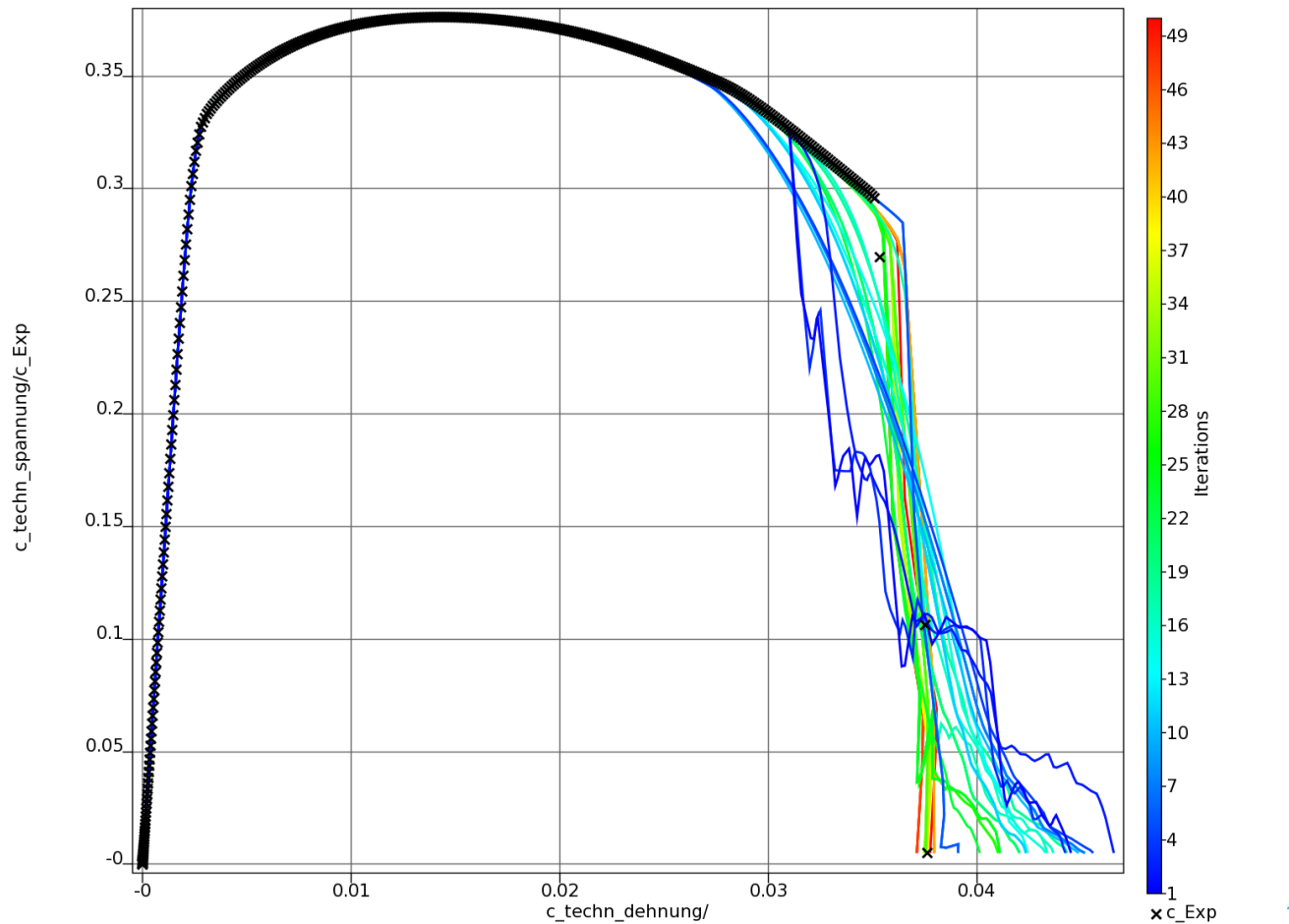
## GA : optimum at each generation



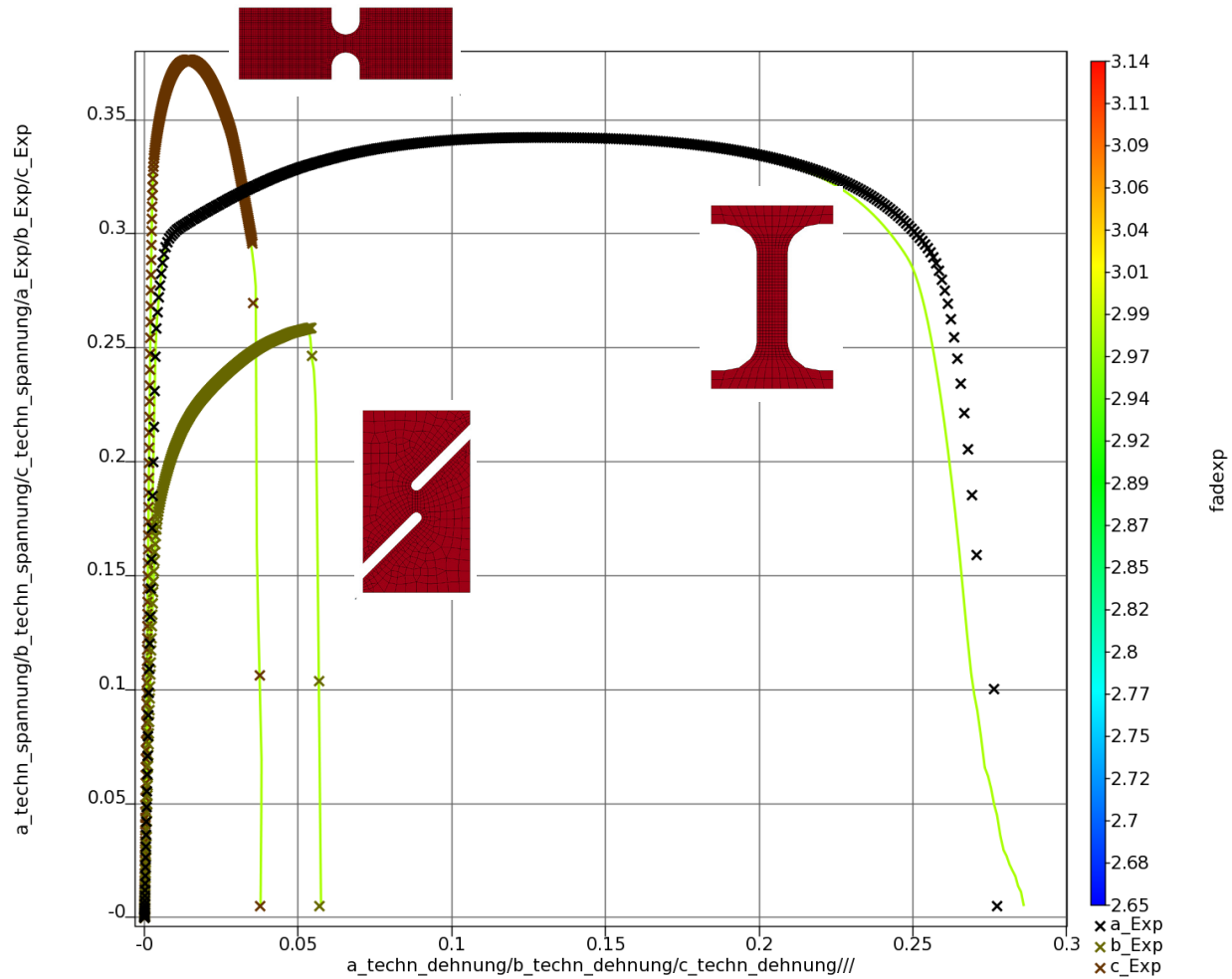


# Case C: tensile (notch)

## GA : optimum at each generation

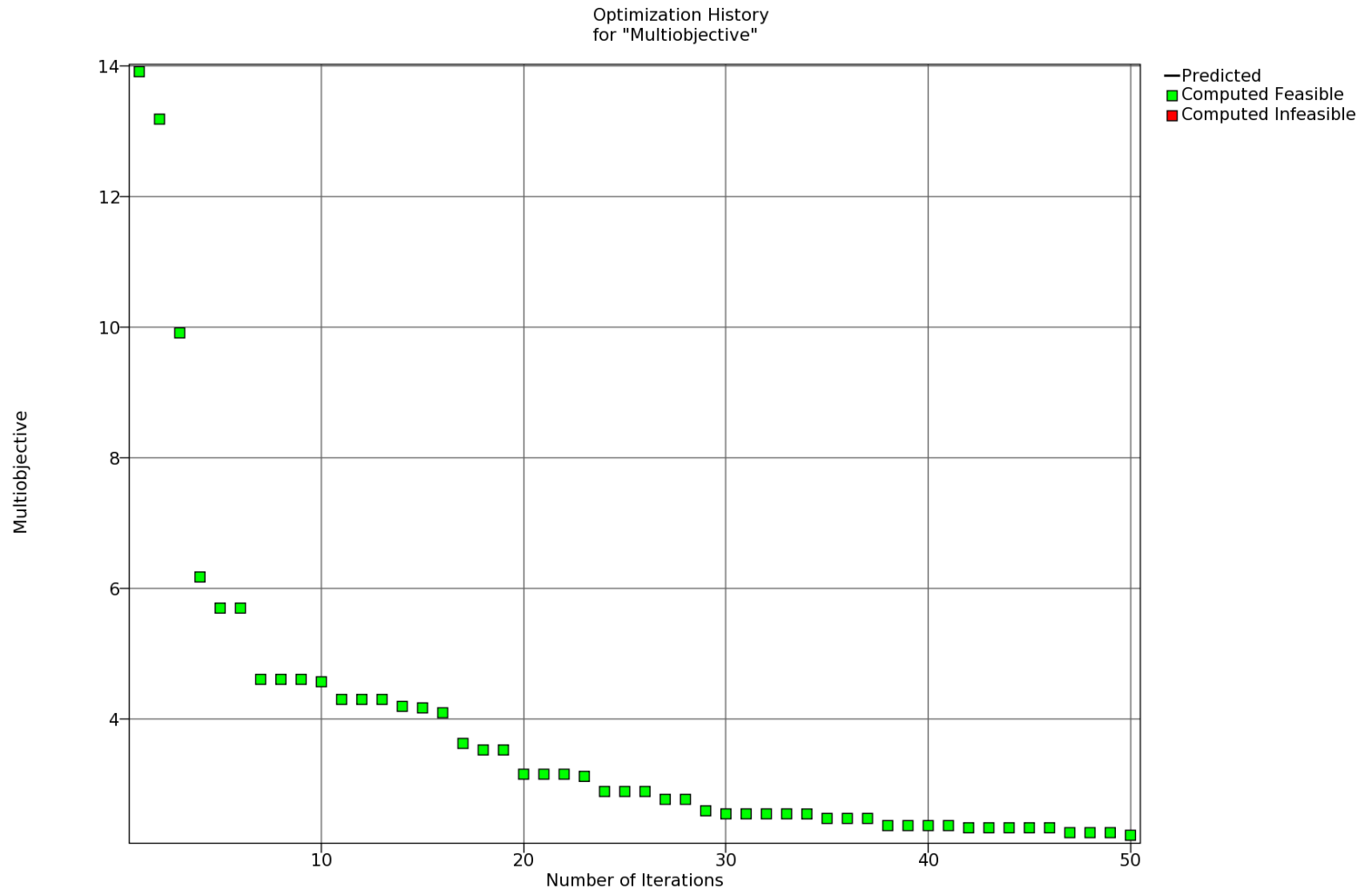


# Optimum (GA/DTW)



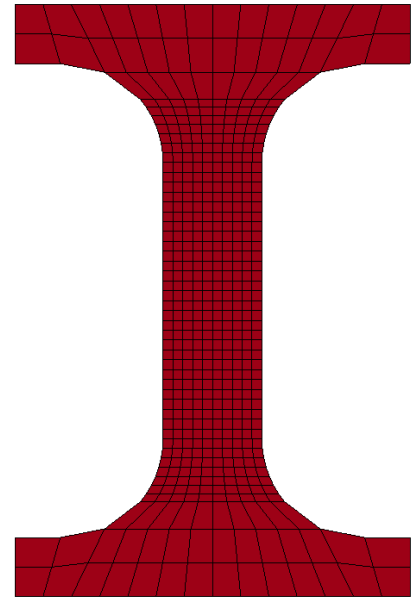
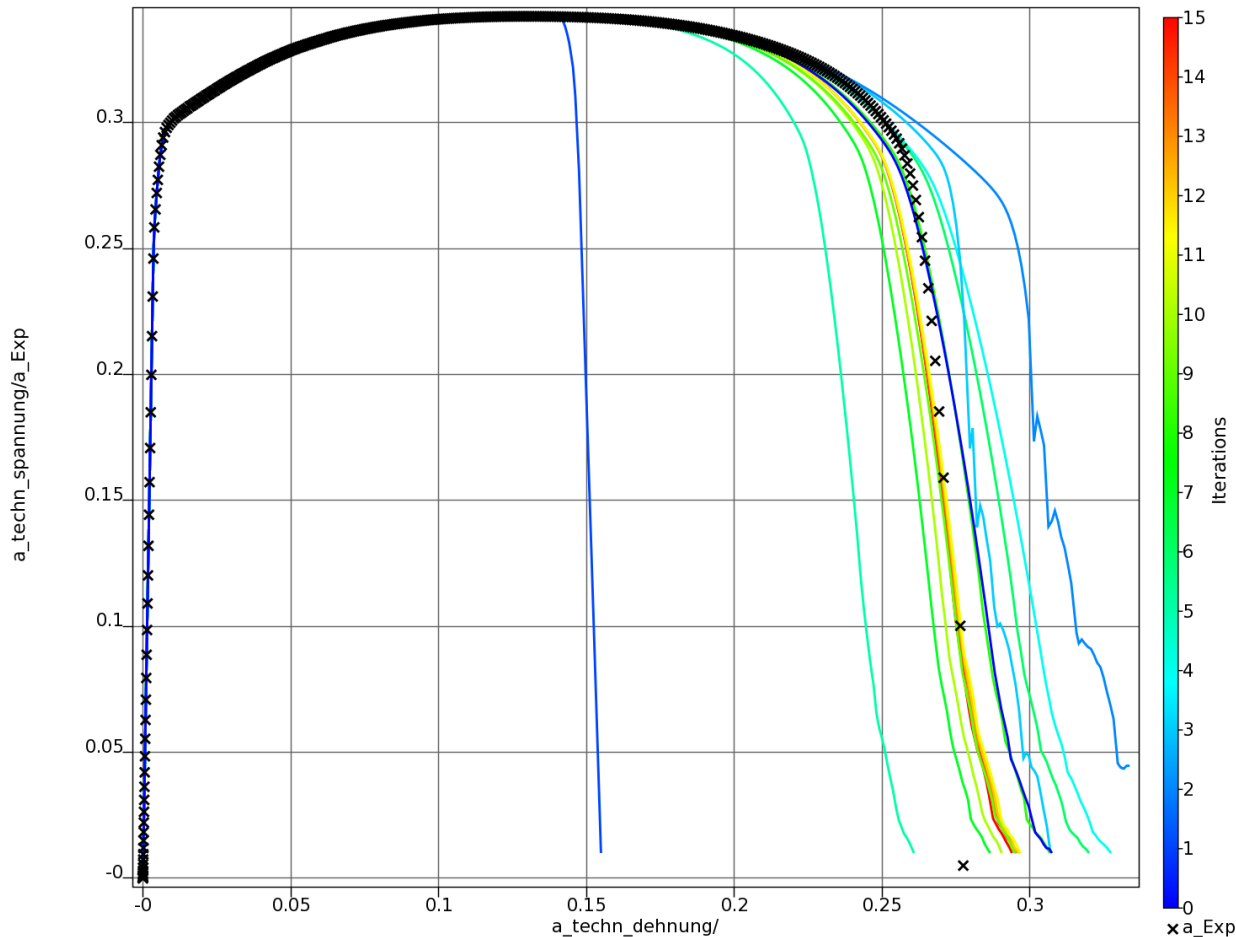
# Optimization history

## GA, DTW distance measure



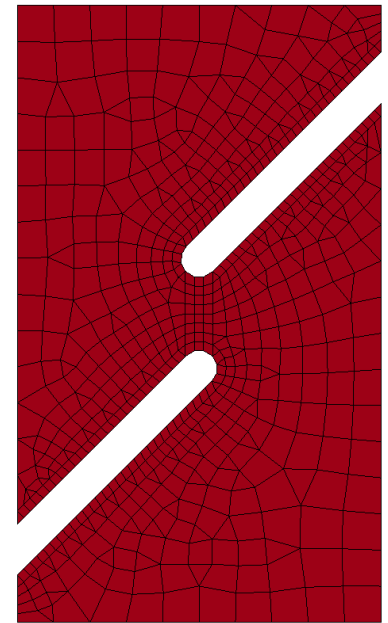
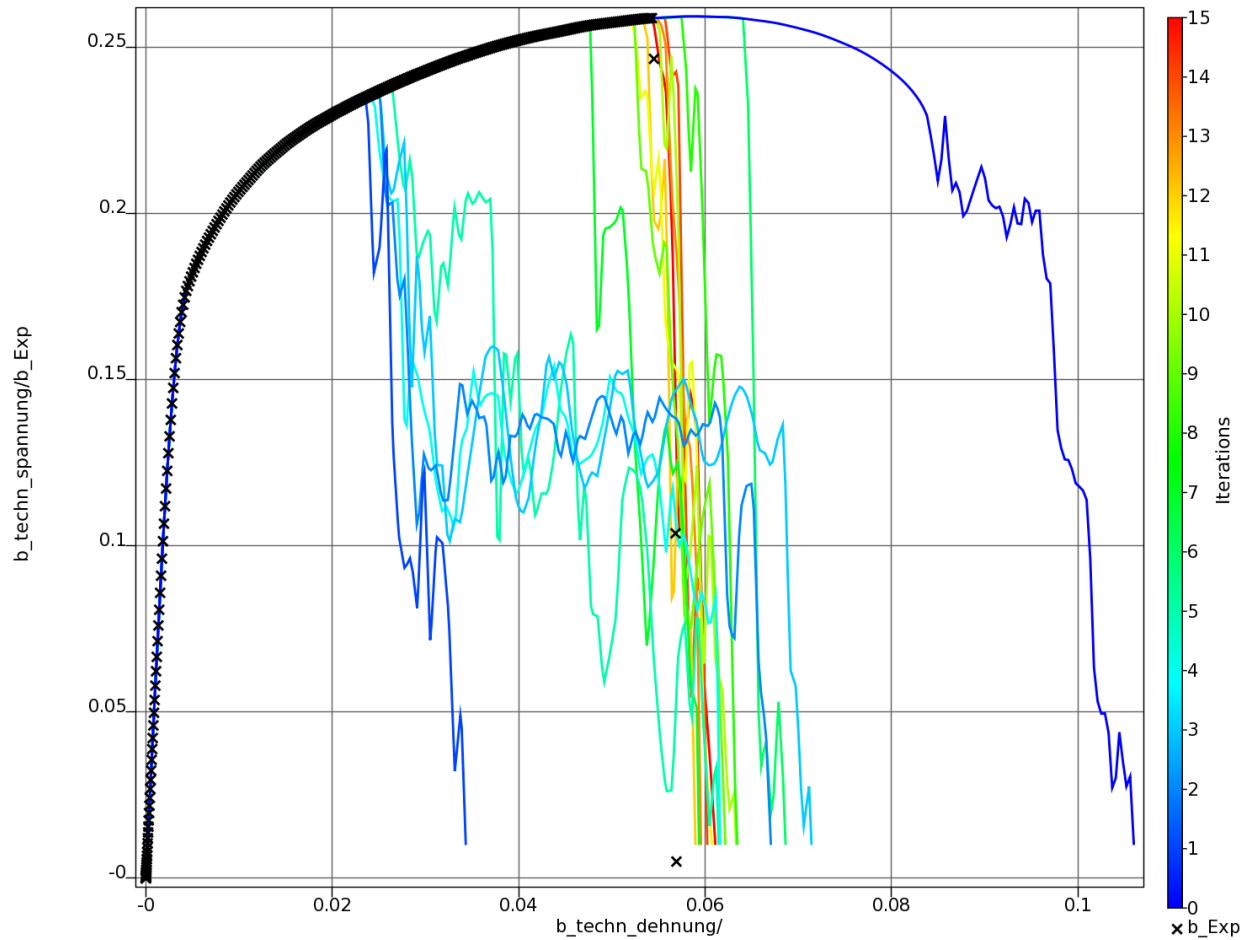
# Case A: tensile

## SRSM: optimum at each iteration



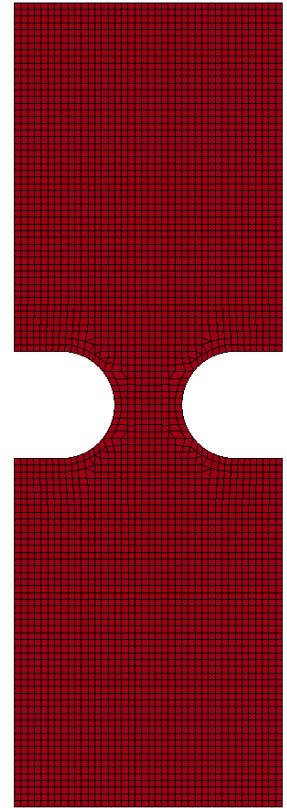
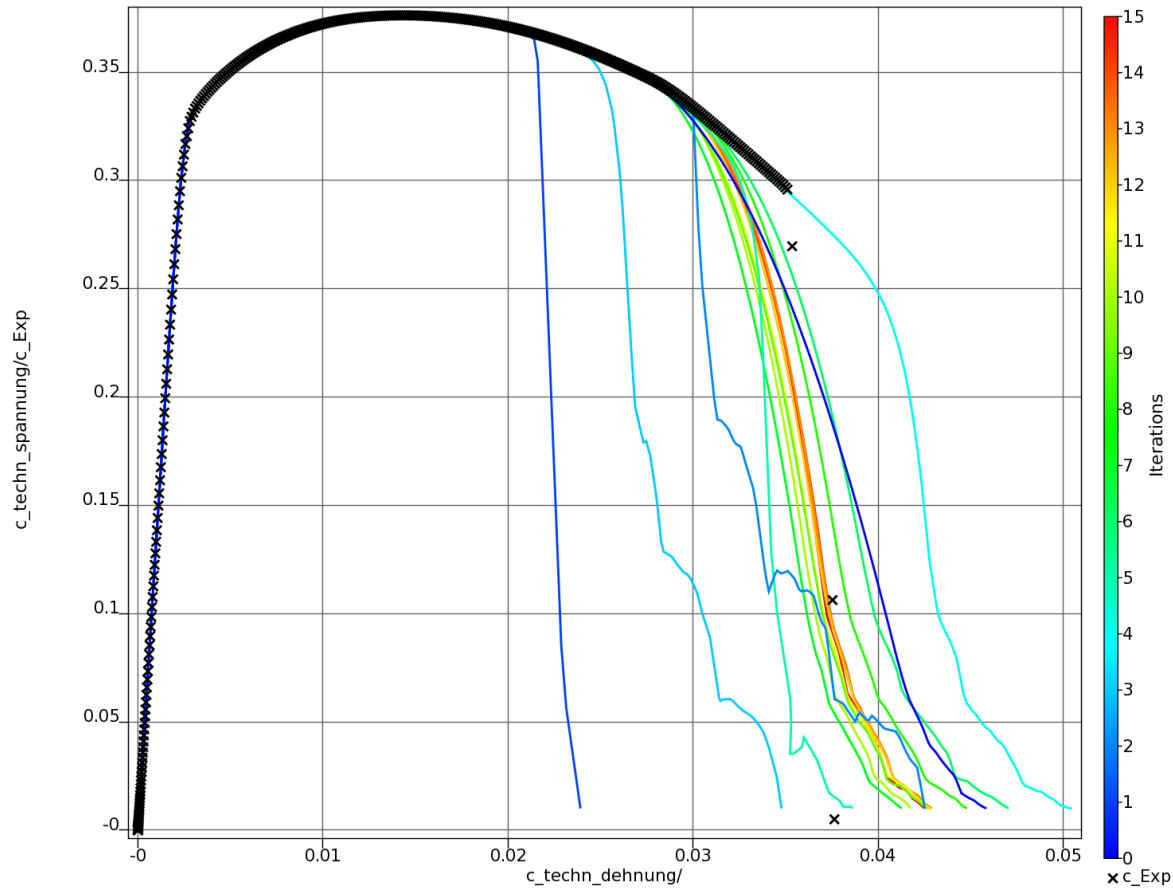
# Case B: shear

## SRSM: optimum at each iteration

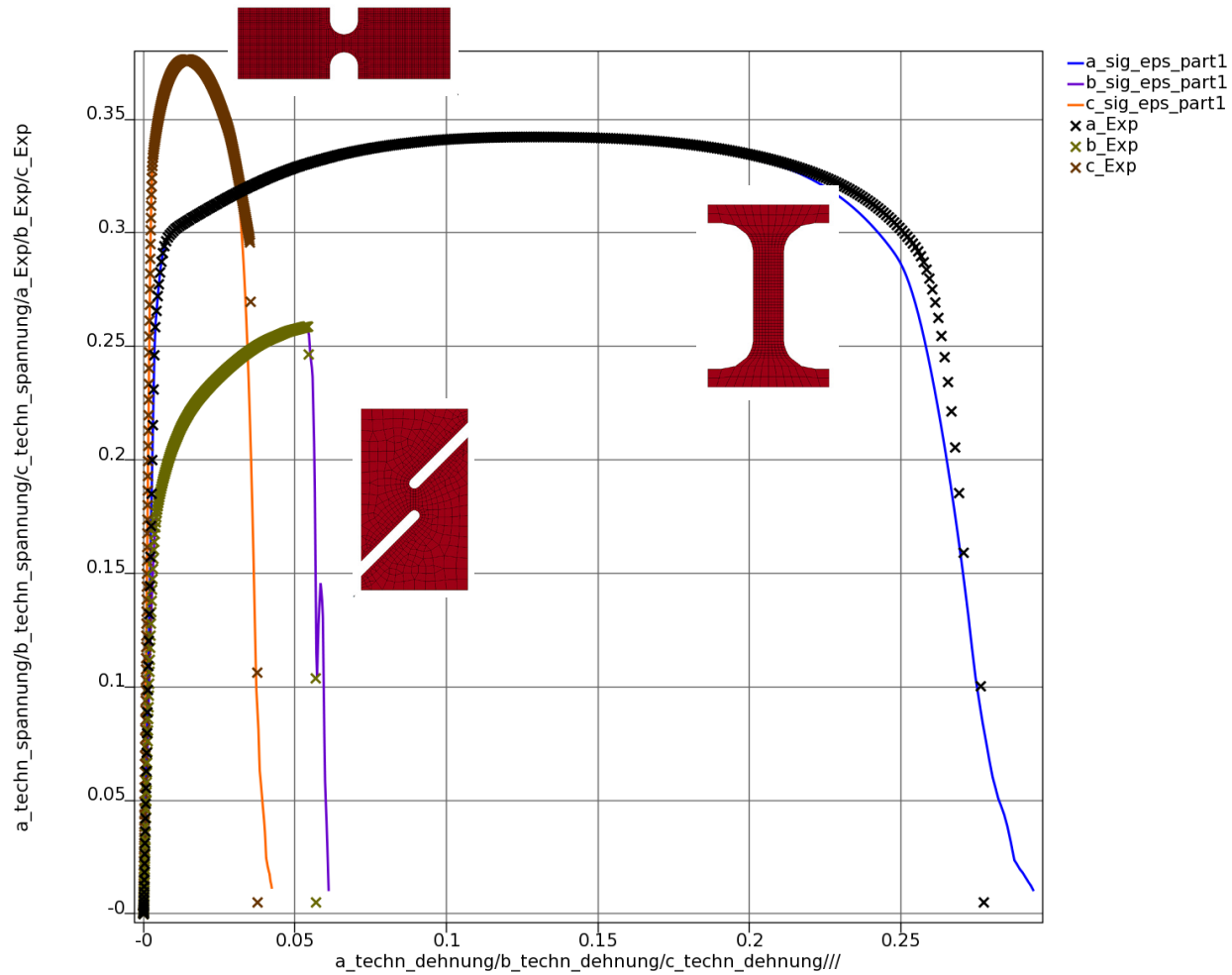


# Case C: tensile (notch)

## SRSM: optimum at each iteration

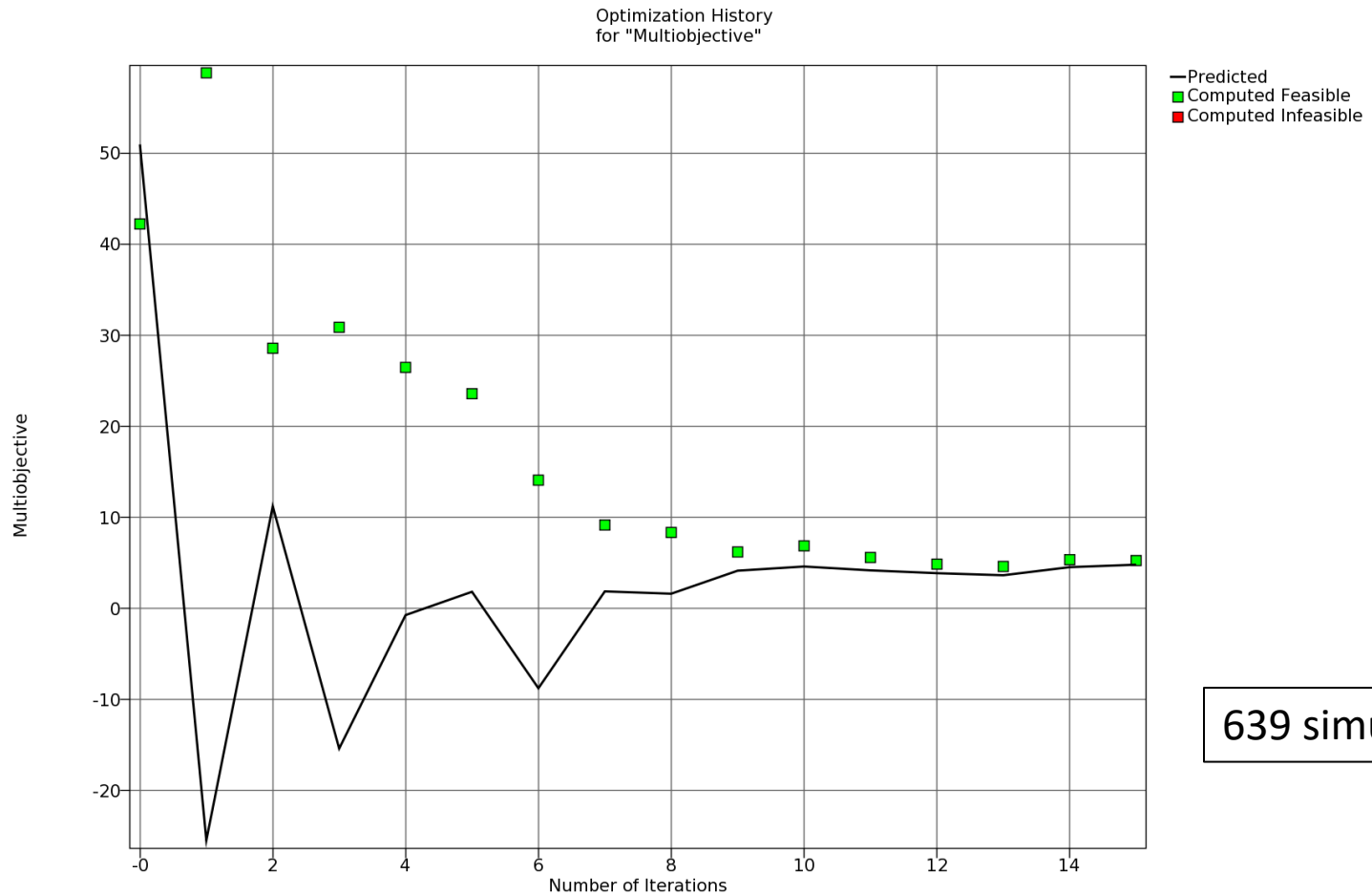


# Optimum (SRSM/DTW)



# Optimization history

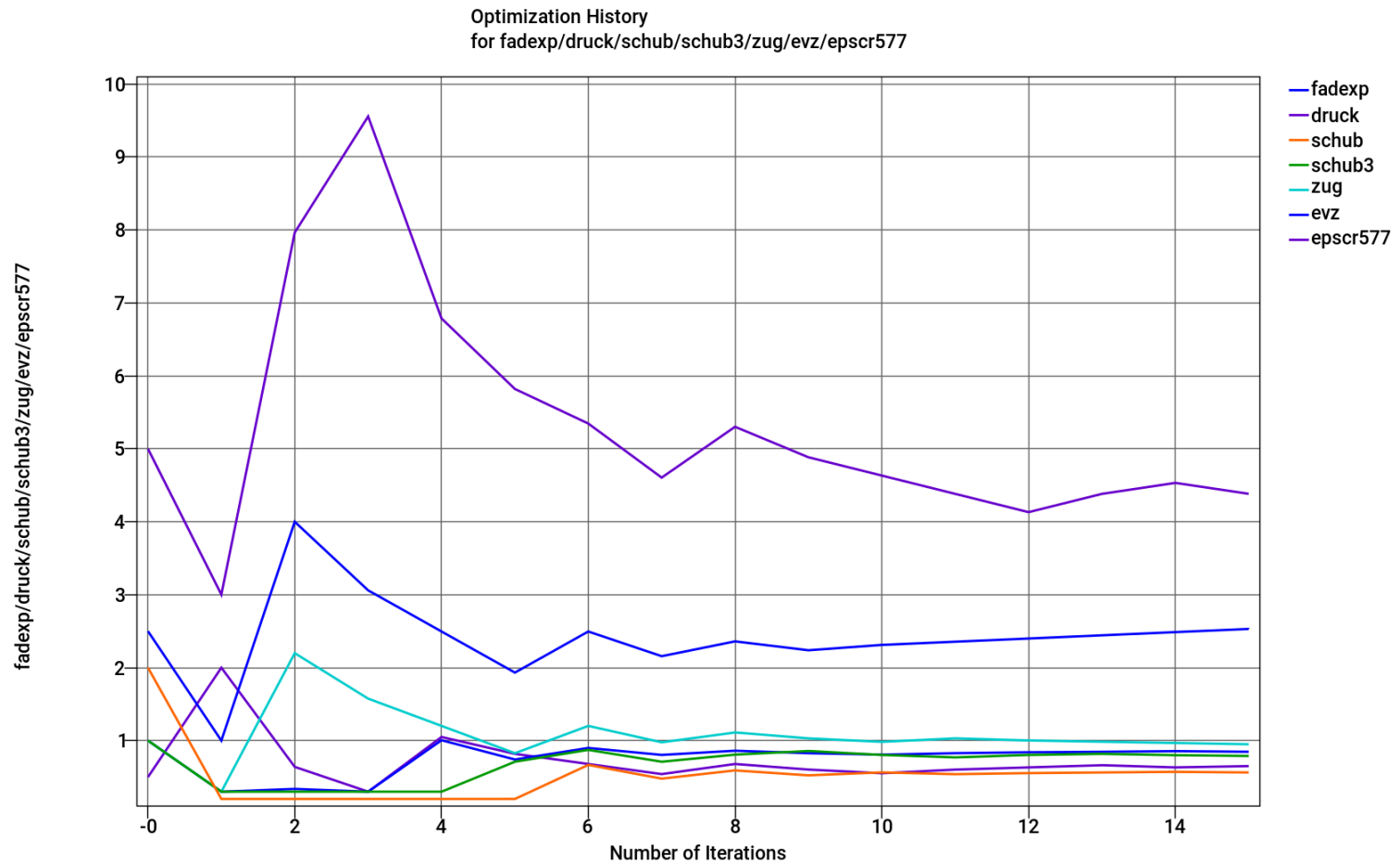
## SRSM, DTW distance measure





# Variable history

## SRSM, DTW distance



# Optimal Parameters

## GA vs. SRSM

	Direct GA	SRSM
Variable		
fadexp	2.9734	2.531
druck	5.12825	4.38299
schub	0.574127	0.563313
schub3	0.435389	0.78979
zug	0.832831	0.950223
evz	0.805032	0.846885
epscr577	0.991622	0.650799
DTW residuals		
a_curve	1.38378	1.17036
b_curve	0.429781	2.34613
c_curve	0.409606	1.75659
<b>Multi-objective</b>	<b>2.22317</b>	<b>5.27307</b>

# Remarks

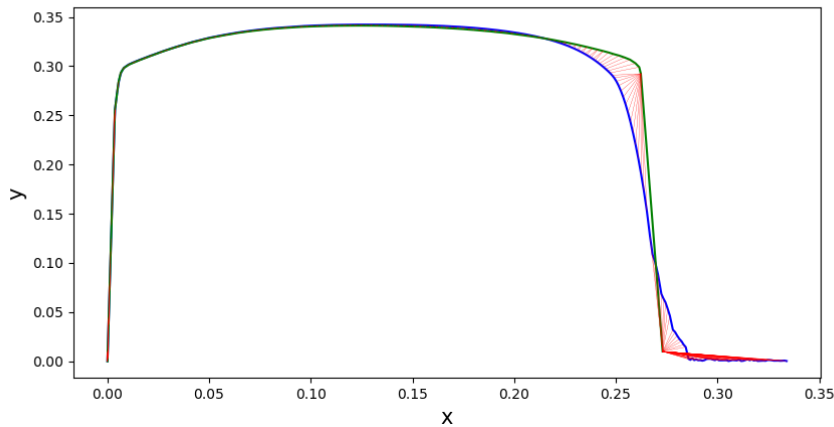
- DTW copes well with *noise* displayed by GISSMO behavior
- DTW requires *Force curve truncation*, using an LS-OPT feature, to avoid oscillation beyond fracture
- DTW easier to use than PCM (Partial Curve Mapping)
  - PCM *fails with noise*, requiring a filter which is not robust
- SRSM (Response Surface) performance compares well with GA (639 vs. 15,000 = 4.3%), despite
  - being a local optimizer
  - having a global convergence deficiency
- Current availability: v6.0 beta

# GISSMO calibration

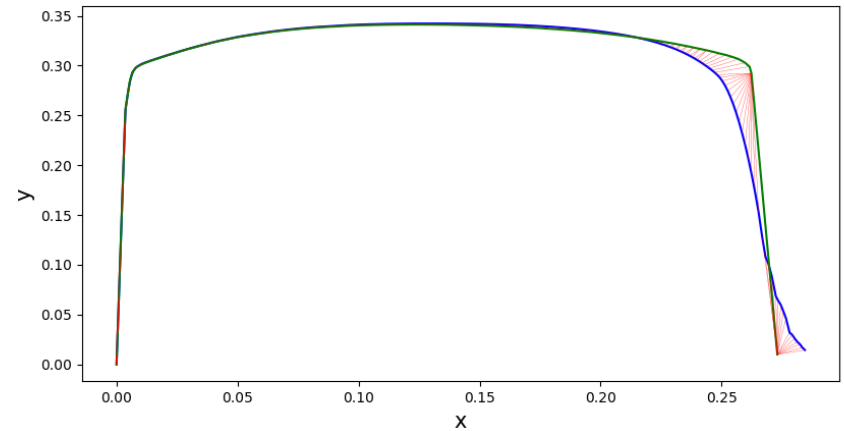
## Recommendations

- Select Dynamic Time Warping as a similarity measure
- Distribute the experimental points uniformly by specifying a number of interpolation points instead of the default
- Truncate the computational force curve  $F$  at failure.
  - This value should be the same as the  $F$  value of the last point in the test curve.
  - DTW requires that the simulated and experimental curves have the same length (or as close as possible), otherwise it may focus on the protruding line segment, and yield a misleading value. (See figures in the Addendum, “DTW: Truncation of the curve”).
- Optimizer:
  - Select SRSM for speed *or*
  - Select Direct GA for global optimality (at roughly  $20 \times$  the cost)

# DTW: Truncation of the curve



**DTW Distance value 5.3**



**Remove the noise on the simulated blue curve at the end. Now the DTW Distance value is 3.4**