

ON QUASILINEAR VISCOELASTIC  
CONSTITUTIVE EQUATIONS

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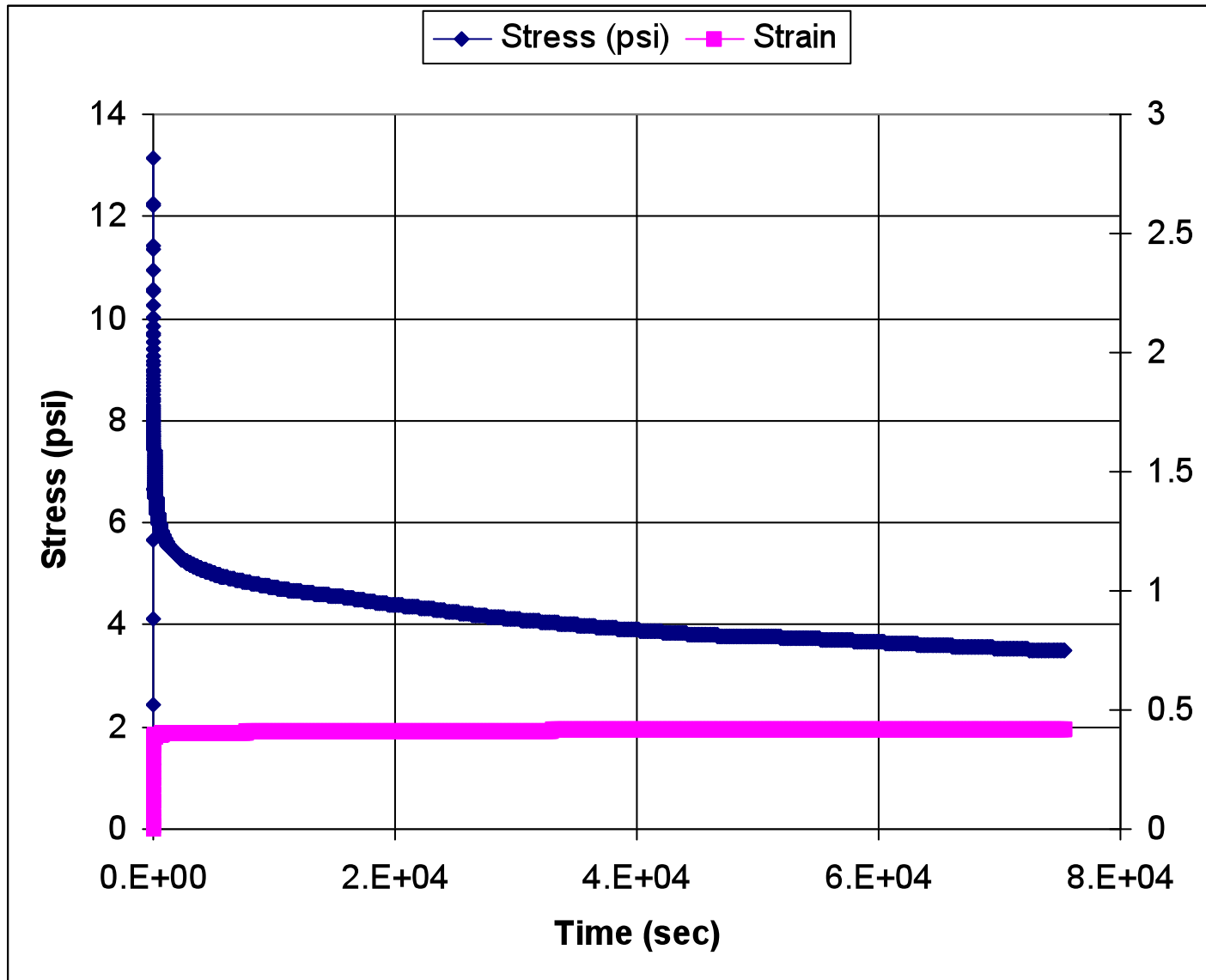
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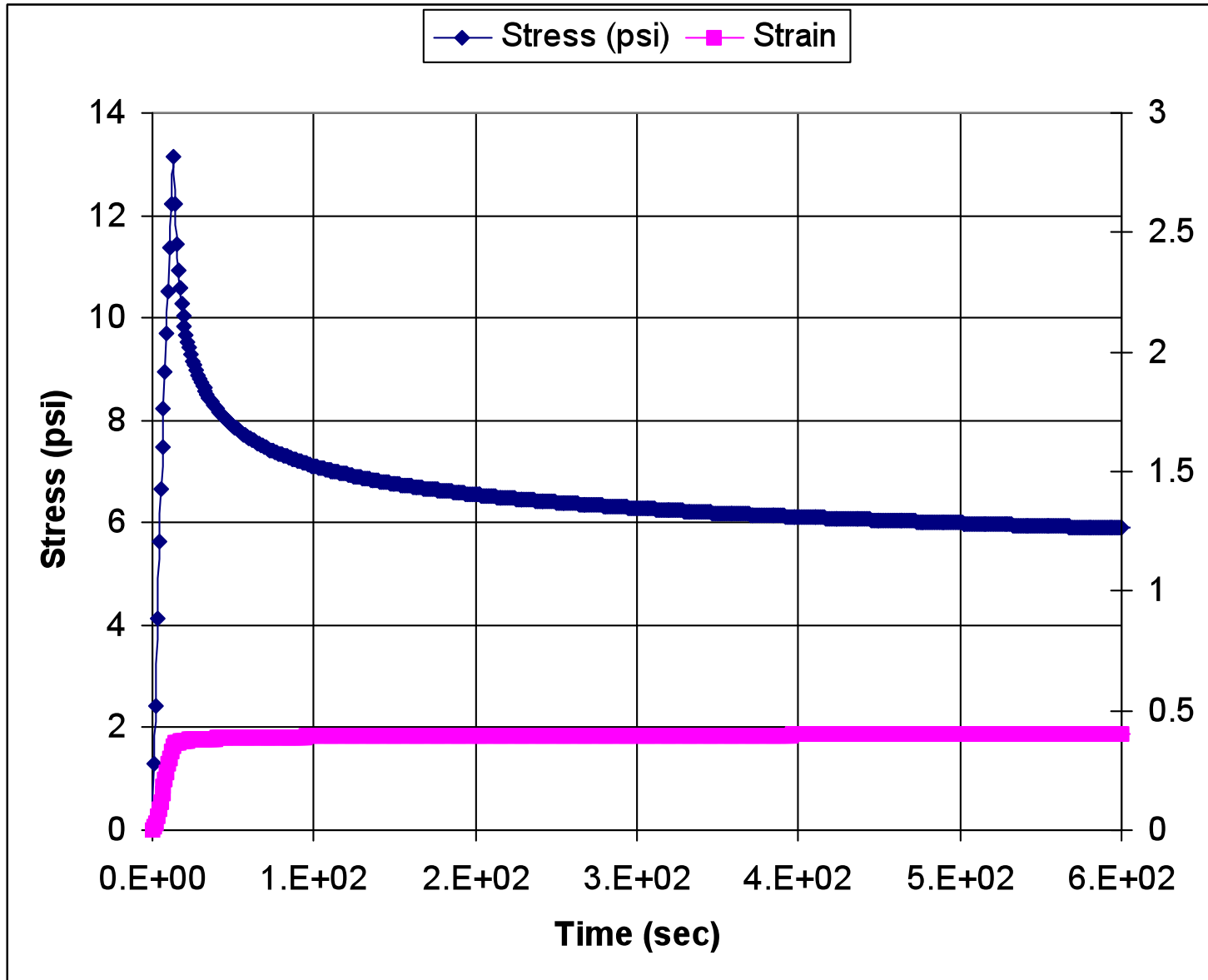
# *Experimental relaxation data*

x



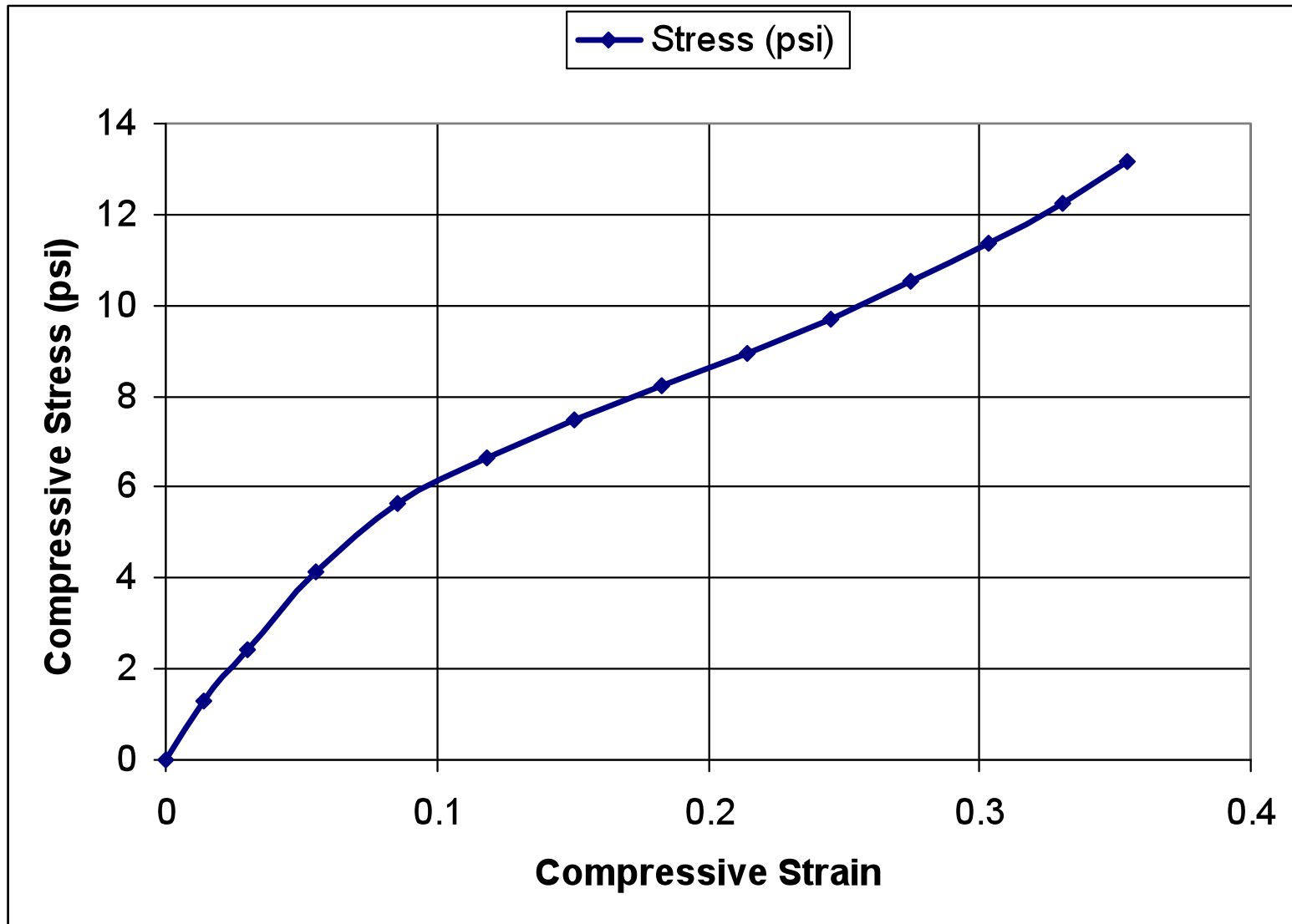
# *Experimental relaxation data*

x

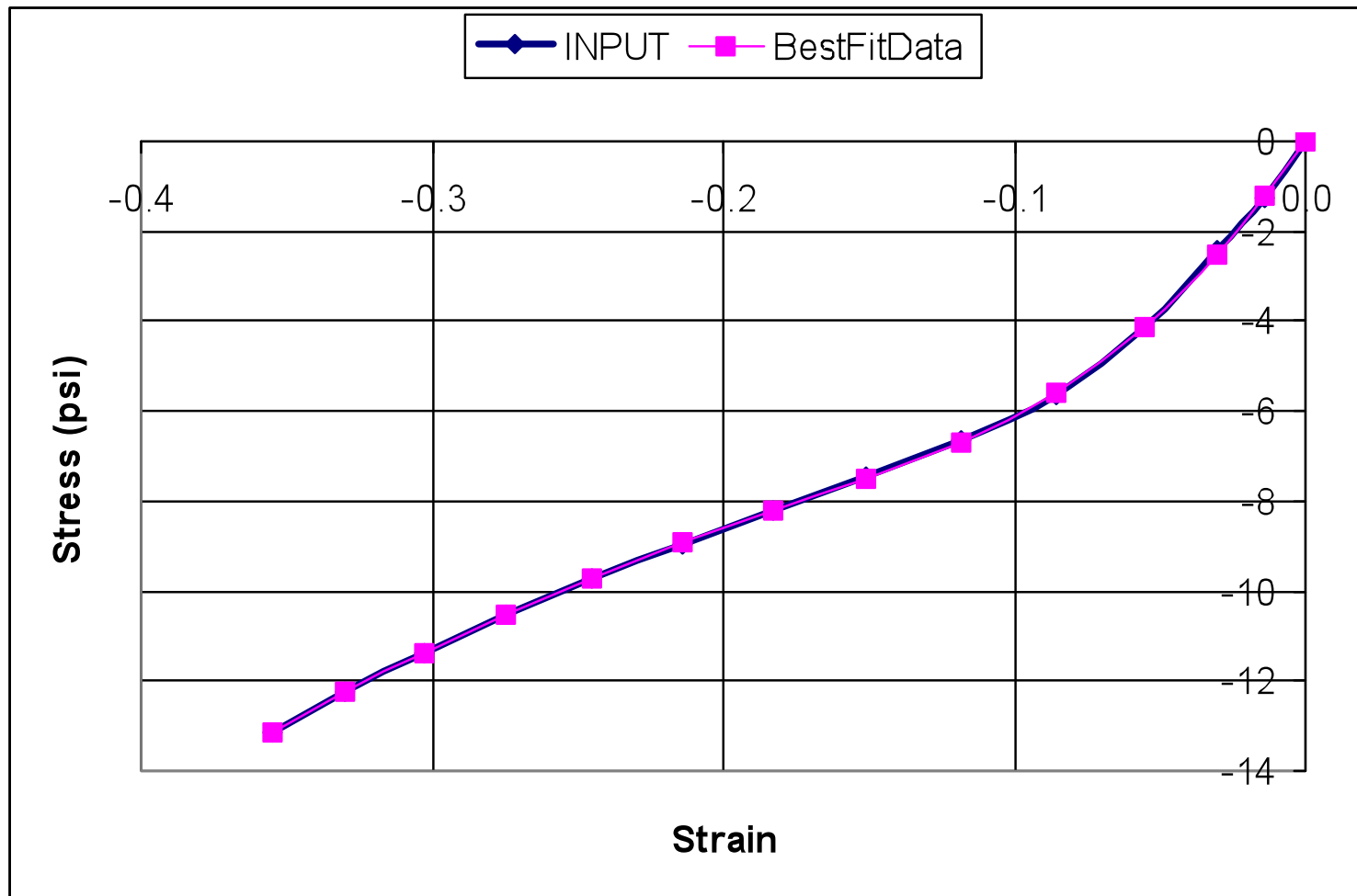


# *Stress-strain curve*

x



# Material constants for the stress-strain curve x



$$C1 = 0.91E+02 \quad C2 = 0.23E+03 \quad C3 = -0.19E+04$$

$$C4 = -0.17E+05 \quad C5 = -0.45E+05 \quad C6 = -0.42E+05$$

Since the relaxation is performed at a strain  $-0.355$  and the measured stress is  $-13.1457$ ; hence, all C's for LS-DYNA must be divided by  $13.1457$ . Or:

$$\begin{aligned} C1 &= 0.692E+01 & C2 &= 0.175E+02 & C3 &= -0.144E+03 \\ C4 &= -0.129E+04 & C5 &= -0.342E+04 & C6 &= -0.319E+04 \end{aligned}$$

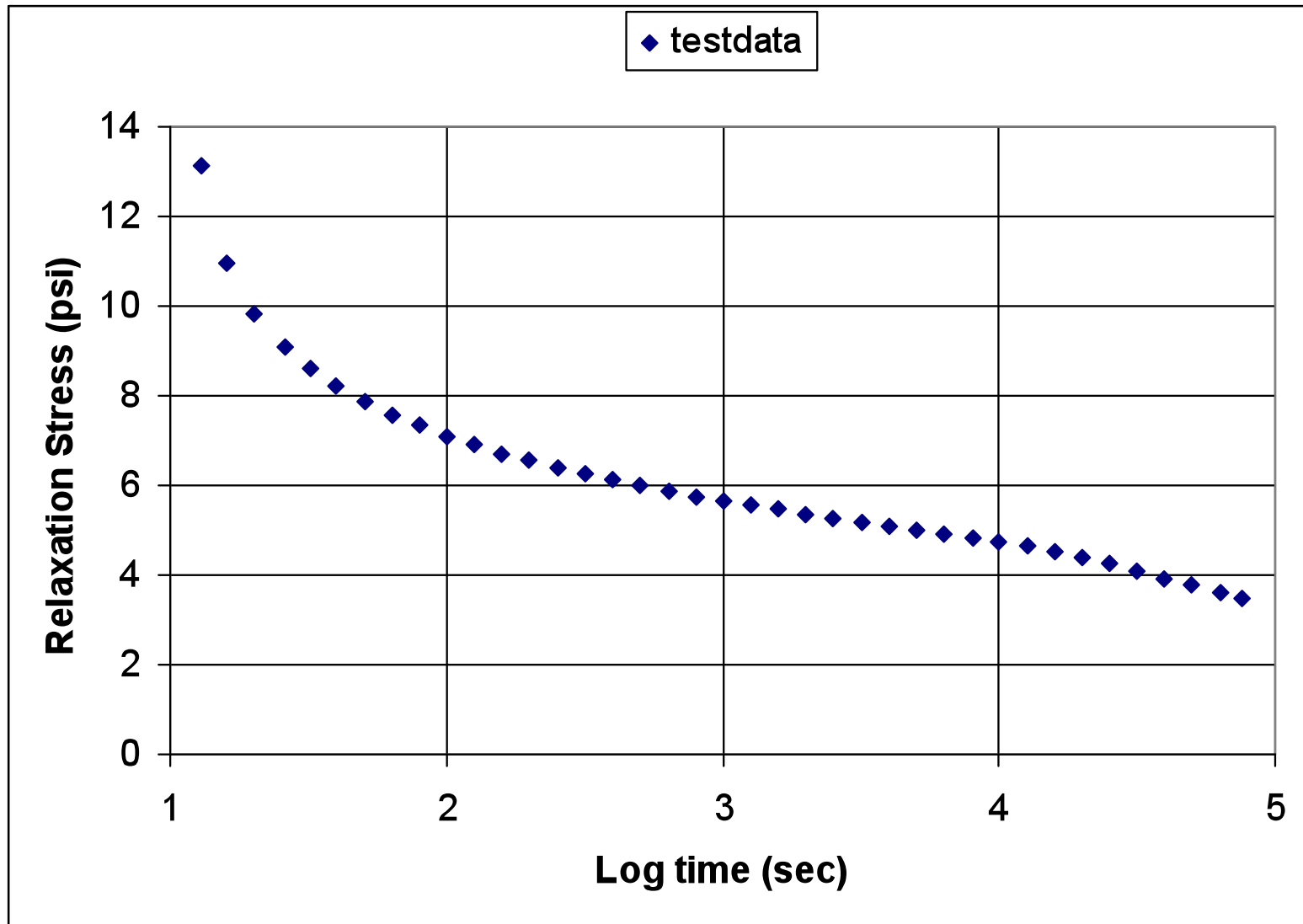
# *Semi-log plot of the experimental relaxation data*

x



# *Selected experimental relaxation data used in the analysis*

x

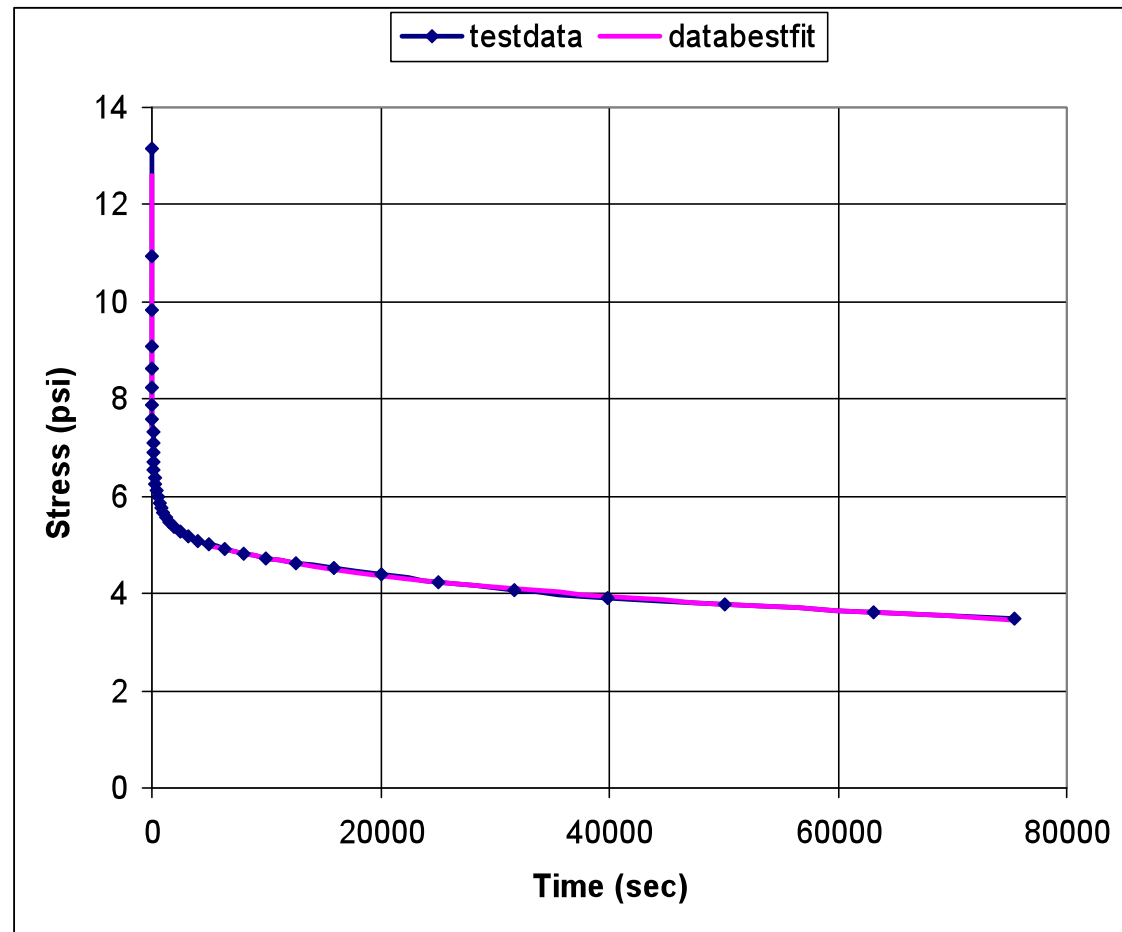




# *Comparison between constitutive equation and test data (35.5% strain)*

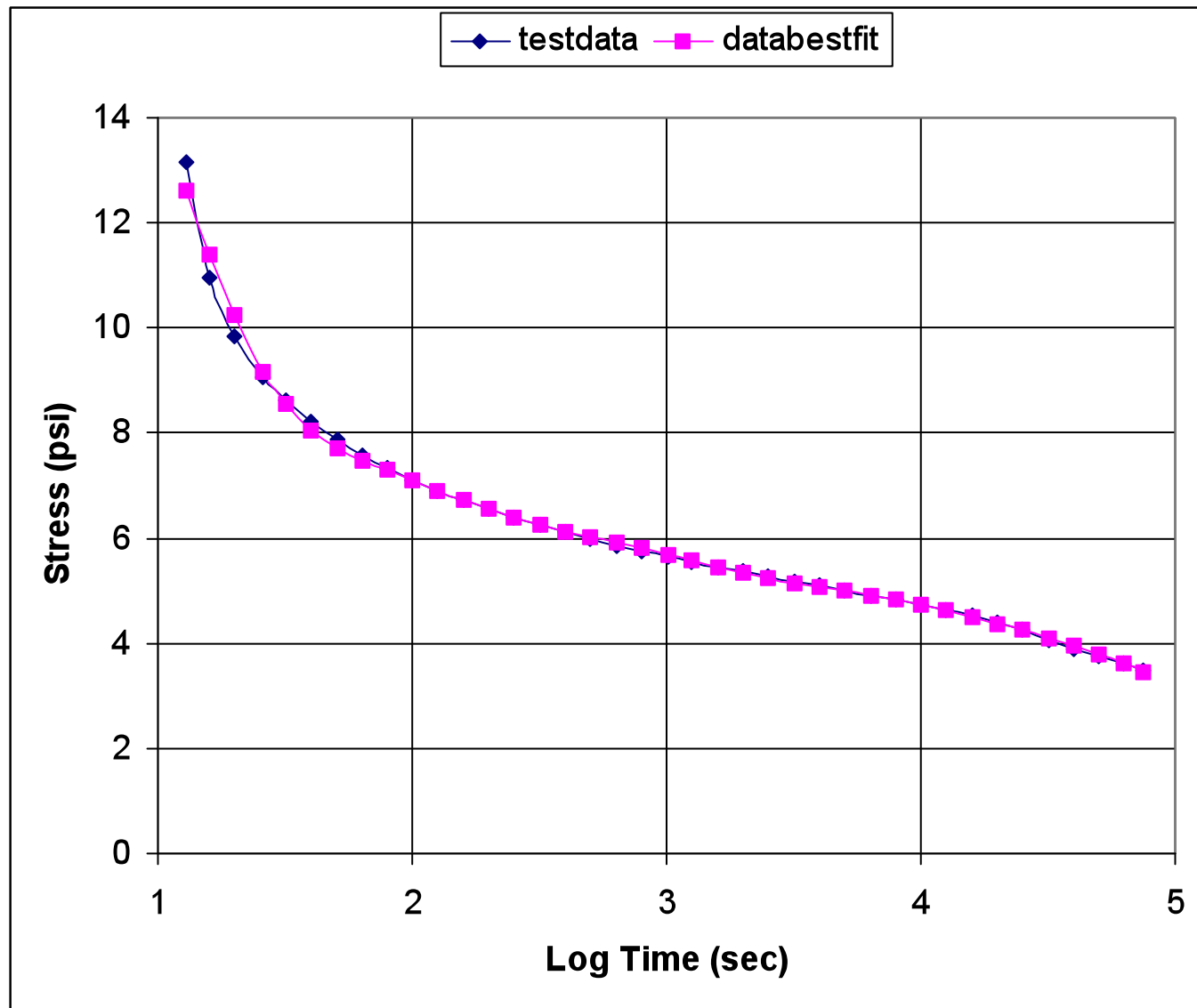
x

$I$	$G(I)$	$BETA(I)$
0	0.2313E+01	0.0000E+00
1	0.2423E+01	0.1000E-04
2	0.6103E+00	0.1000E-03
3	0.1167E+01	0.1000E-02
4	0.1939E+01	0.1000E-01
5	0.1613E+02	0.1000E+00



# *Comparison between constitutive equation and test data (35.5% strain)*

x



*All G's must be divided by 0.355 and 2\*(1+nu)  
for LS-DYNA input.*

<i>I</i>	<i>G(I)</i>	<i>BETA(I)</i>
<i>0</i>	<i>6.515E+00</i>	<i>0.0000E+00</i>
<i>1</i>	<i>6.825E+01</i>	<i>0.1000E-04</i>
<i>2</i>	<i>1.7192E+00</i>	<i>0.1000E-03</i>
<i>3</i>	<i>32873E+00</i>	<i>0.1000E-02</i>
<i>4</i>	<i>5.4620E+00</i>	<i>0.1000E-01</i>
<i>5</i>	<i>4.5437E+01</i>	<i>0.1000E+00</i>

# Material constants for LS-DYNA

x

$$C1 = 0.692E+01 \quad C2 = 0.175E+02 \quad C3 = -0.144E+03$$

$$C4 = -0.129E+04 \quad C5 = -0.342E+04 \quad C6 = -0.319E+04$$

<i>I</i>	<i>G(I)</i>	<i>BETA(I)</i>
<i>0</i>	<i>6.515E+00</i>	<i>0.0000E+00</i>
<i>1</i>	<i>6.825E+01</i>	<i>0.1000E-04</i>
<i>2</i>	<i>1.7192E+00</i>	<i>0.1000E-03</i>
<i>3</i>	<i>32873E+00</i>	<i>0.1000E-02</i>
<i>4</i>	<i>5.4620E+00</i>	<i>0.1000E-01</i>
<i>5</i>	<i>4.5437E+01</i>	<i>0.1000E+00</i>